# **FREQUENCIES**

If the absolute value of any observation is greater than  $10^{13}$ , no calculations are done. For sorting of the observations, see Appendix 6. For information on percentiles for grouped data, see Appendix 8.

### **Notation**

The following notation is used throughout this chapter unless otherwise stated:

$X_{l}$	Value of the	variable for	case k
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 $w_k$  Weight for case k

NV Number of distinct values the variable assumes

Number of cases

W Sum of weights of the cases

### **Basic Statistics**

The values are sorted into ascending order and the following calculated:

Sum of Weights of Cases Having Each Value of X

$$f_j = \sum_{i=1}^{N} w_i k_i$$
  $j = 1, 2, ..., NV$ 

where

$$k_i = \begin{cases} 1 & \text{if } X_i = X_j \\ 0 & \text{otherwise} \end{cases}$$

where  $X_j$  is the *j*th largest distinct value of X.

#### **2** FREQUENCIES

#### Relative Frequency (Percentage) for each Value of X

$$Rf_j = \left(\frac{f_j}{W'}\right) \times 100$$

where

$$W' = \sum_{i=1}^{NV} f_i$$
 (sum over all categories including those declared as missing values)

#### **Adjusted Frequency (Percentage)**

$$Af_j = \left(\frac{f_j}{W}\right) \times 100$$

where

$$W = \sum_{i=1}^{NV} f_i k_i$$
 (sum over nonmissing categories)

and

$$k_i = \begin{cases} 0 & \text{if } X_i \text{ has been declared missing} \\ 1 & \text{otherwise} \end{cases}$$

For all  $X_j$  declared missing, an adjusted frequency is not printed.

#### **Cumulative Frequency (Percentage)**

$$Cf_j = \sum_{i=1}^{j} f_i$$

#### Minimum

$$\min_{k} X_k$$

#### Maximum

$$\max_{k} X_k$$

#### Mode

Value of  $X_j$  which has the largest observed frequency. If several are tied, the smallest value is selected.

#### Range

Maximum – Minimum

#### The pth percentile

Find the first score interval (x2) containing more than tp cases.

$$p \text{th percentile} = \begin{cases} x_2 & \text{if } tp - cp_1 \ge 100/W \\ \left\{ 1 - \left[ (W+1) \, p/100 - cc_1 \right] \right\} x_1 & \text{if } tp - cp_1 < 100/W \\ + \left[ (W+1) \, p/100 - cc_1 \right] x_2 \end{cases}$$

where

$$tp = (W+1) p/100$$

$$cp_1 < tp < cp_2$$

 $x_1$  and  $x_2$  are the values corresponding to  $cp_1$  and  $cp_2$ , respectively  $cc_1$  is the cumulative frequency up to  $x_1$ 

 $cp_1$  is the cumulative percent up to  $x_1$ 

#### 4 FREQUENCIES

Mean

$$\overline{X} = \frac{\displaystyle\sum_{j=1}^{NV} f_j X_j}{W}$$

Moments about the mean are calculated as:

$$M_{j} = \sum_{i=1}^{NV} f_{i} (X_{i} - \overline{X})^{j}$$
  $j = 2, 3, 4$ 

Variance

$$S^2 = \frac{M_2}{(W-1)}$$

**Standard Deviation** 

$$S = \sqrt{S^2}$$

Standard Error of the Mean

$$SEM = \frac{S}{\sqrt{W}}$$

Skewness (computed if  $\textit{W} \geq 3$  and  $\textit{S}^2 > 0$ ) (Bliss, 1967, p. 144)

$$g_1 = \frac{WM_3}{(W-1)(W-2)S^3}$$
  $se(g_1) = \sqrt{\frac{6W(W-1)}{(W-2)(W+1)(W+3)}}$ 

Kurtosis (computed if  $W \ge 4$  and  $S^2 > 0$ )

$$g_2 = \frac{W(W+1)M_4 - 3(W-1)M_2^2}{(W-1)(W-2)(W-3)S^4} \qquad se(g_2) = \sqrt{\frac{4(W^2 - 1)se(g_1)^2}{(W-3)(W+5)}}$$

## **References**

Blalock, H. M. 1972. Social statistics. New York: McGraw-Hill.

Bliss, C. I. 1967. Statistics in biology, Volume 1. New York: McGraw-Hill.