

Illustration of Euler's Identity:

$$e^{i\pi} + 1 = 0$$

$$e = \lim_{n \rightarrow \infty} (1 + 1/n)^n = 2.71828$$

$$e^x = \lim_{n \rightarrow \infty} (1 + x/n)^n = \lim_{n \rightarrow \infty} [(1 + 1/n)^n]^x \quad \leftarrow \text{(someone please explain why this is)}$$

$$e^{i\pi} = \lim_{n \rightarrow \infty} (1 + i\pi/n)^n$$

n	$(1 + i\pi/n)^n$	Complex Result	Real Part	Imaginary Part
1	$(1 + i\pi/1)^1 =$	1.00000 + i * 3.14159	+1.00000	3.14159
2	$(1 + i\pi/2)^2 =$	-1.46740 + i * 3.14159	-1.46740	3.14159
3	$(1 + i\pi/3)^3 =$	-2.28987 + i * 1.99321	-2.28987	1.99321
4	$(1 + i\pi/4)^4 =$	-2.32060 + i * 1.20370	-2.32060	1.20370
5	$(1 + i\pi/5)^5 =$	-2.16857 + i * 0.75902	-2.16857	0.75902
6	$(1 + i\pi/6)^6 =$	-2.00552 + i * 0.50677	-2.00552	0.50677
7	$(1 + i\pi/7)^7 =$	-1.86707 + i * 0.35638	-1.86707	0.35638
8	$(1 + i\pi/8)^8 =$	-1.75537 + i * 0.26174	-1.75537	0.26174
9	$(1 + i\pi/9)^9 =$	-1.66578 + i * 0.19919	-1.66578	0.19919
10	$(1 + i\pi/10)^{10} =$	-1.59336 + i * 0.15606	-1.59336	0.15606
100	$(1 + i\pi/100)^{100} =$	-1.05056 + i * 0.00109	-1.05056	0.00109
1,000	$(1 + i\pi/1,000)^{1,000} =$	-1.00495 + i * 1.03865 E-5	-1.00495	1.03865 E-5
10,000	$(1 + i\pi/10,000)^{10,000} =$	-1.00049 + i * 1.03405 E-7	-1.00049	1.03405 E-7
100,000	$(1 + i\pi/100,000)^{100,000} =$	-1.00005 + i * 1.03359 E-9	-1.00005	1.03359 E-9
210,690	$(1 + i\pi/210,690)^{210,690} =$	-1.00002 + i * 2.32836 E-10	-1.00002	2.32836 E-10
210,691	$(1 + i\pi/210,691)^{210,691} =$	-1.00002 + i * 0	-1.00002	0
1,000,000	$(1 + i\pi/1,000,000)^{1,000,000} =$	-1.00000 + i * 0	-1	0
$n \rightarrow \infty$	$(1 + i\pi/n)^n =$	-1.00000 + i * 0	-1	0

$$e^{i\pi} = \lim_{n \rightarrow \infty} (1 + i\pi/n)^n = \mathbf{-1}$$

$$e^{i\pi} = \mathbf{-1}$$

$$e^{i\pi} + 1 = \mathbf{0}$$