

$$n(1+x)^{n-1} = \binom{n}{1} + 2\binom{n}{2}x + \dots + r\binom{n}{r}x^{r-1} + \dots + nx^{n-1}$$