

# Calculation report

## 1. Critical analysis of the stresses in the driven shaft

**Parameters:**

$Mg = 7.85N$

Suppose weight distribution evenly spread over 4 wheels when vehicle speed and acceleration = 0

The normal force of every wheel:  $F_N = 1.96N$

Distance between wheels is 23cm.

Distance between left wheel and gear is 11.5.

Distance between left wheel and bearing is 3cm.

Distance between right wheel and gear is 11.5cm.

Distance between right wheel and bearing is 3cm

Radius spur gear,  $r_s = 2.1cm$

Radius pinion gear,  $r_p = 0.25cm$

Radius wheel  $r_w = 4cm$

So first of all we need to calculate the force transferred from the motor to the first gear.

$$T_M = 8,55 * 70\% * I * 10^{-3} (Nm)$$

With  $T$  = Torque from the motor.

$$I = 0,9 A$$

Torque constant: 8,55 mNm/A

Constant Efficiency: 70%

The torque from the motor is than:

$$T_M = 0,00539 Nm$$

Calculation:

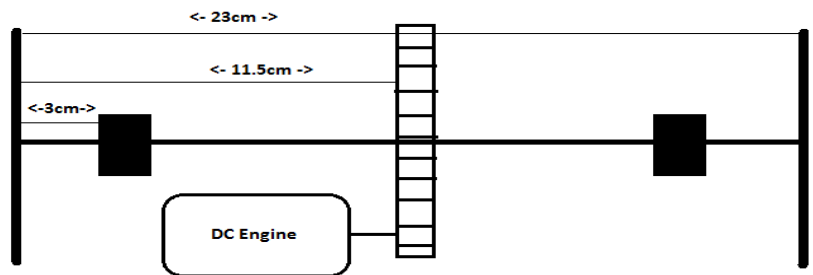
**Torsion stress to shear stress**

The torque of shaft:

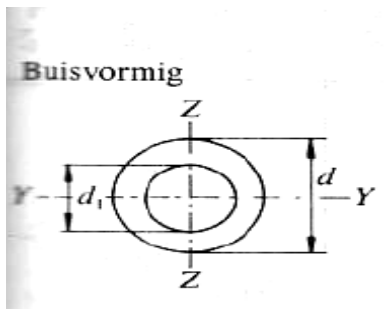
$$T_s = T_M * r_s / r_p = 0.0453 Nm$$

So the torque of wheel:

$$T_w = T_s / 2 = 0.0226 Nm$$

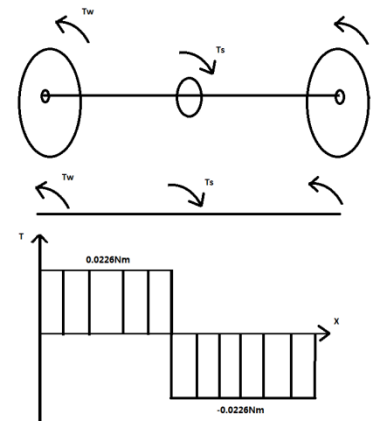


Our shaft is made by Aluminium and hollow. The  $D = 5mm$  and  $d = 4.5mm$



$$I_y = I_z = \frac{\pi(d^4 - d_1^4)}{64}$$

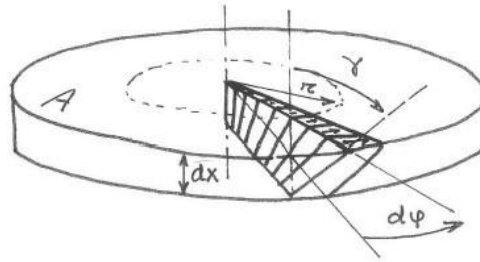
$$I_p = \frac{\pi(d^4 - d_1^4)}{32}$$



$$M_w = I_p * G * \phi$$

$$I_p = \frac{\pi \times (0.005^4 - 0.0045^4)}{32} = 2.11 \times 10^{-11} m^4$$

$$\tau_{max} = \frac{T \times R}{I_p} = 2.68 MPa$$



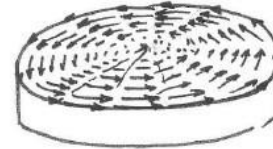
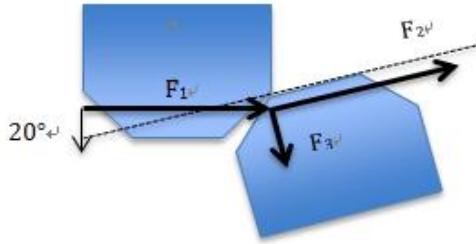
$$r d\phi = \gamma dx$$

$$\tau = G \cdot \gamma$$

$$\tau = G \cdot r \frac{d\phi}{dx}$$

$$\tau = G \cdot r \cdot \phi$$

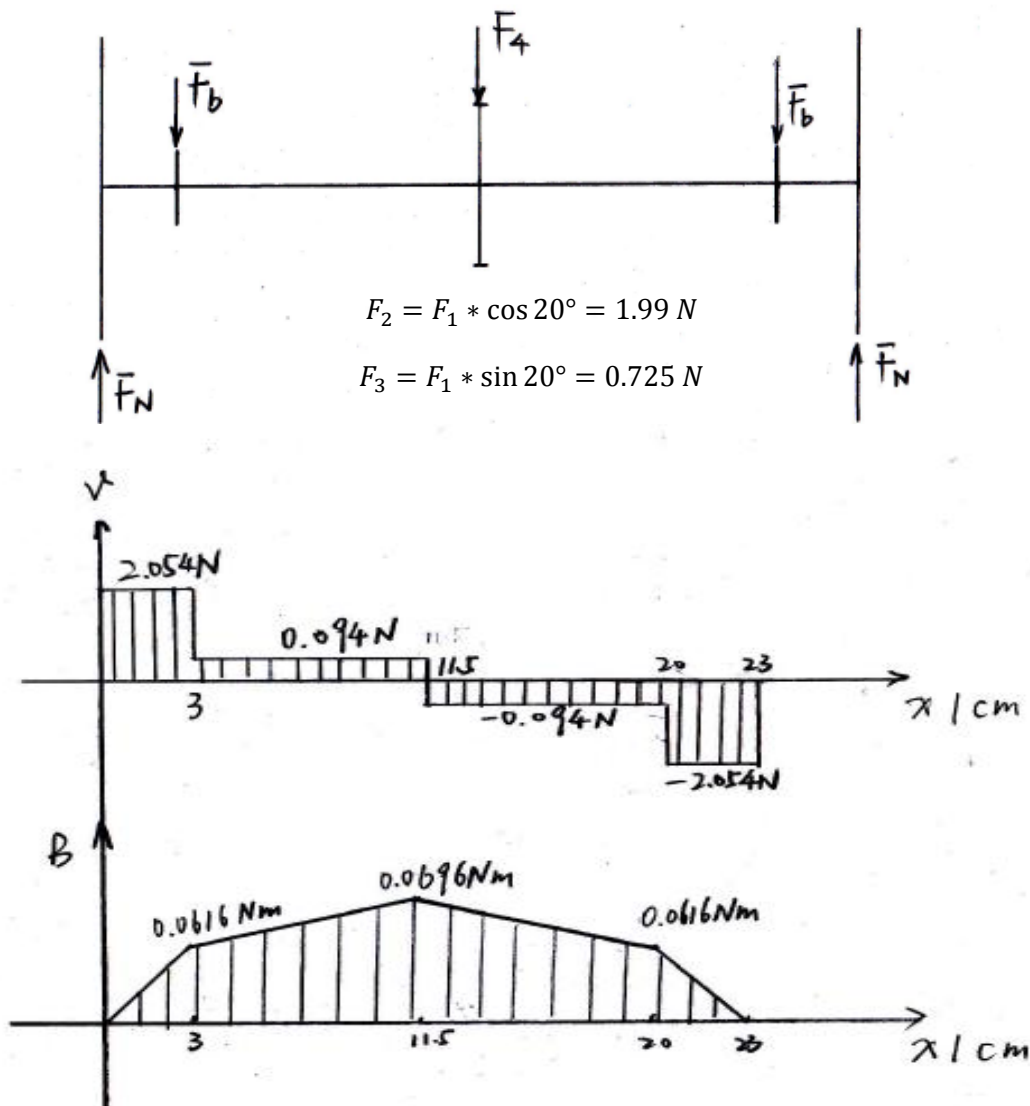
**Bending stress**



We now look at the forces generated by the pinion gear as a result of the gear teeth's contact area being at an angle of 20° to the plane connecting the centers of the 2 gears.

$$\text{So } F_p = \frac{T_M}{r_p} = 2.12 N$$

Now that we know the force from the smallest gear, we will be able to find the forces on the second and bigger gear due to the smaller gear.



**Graph2**

Therefore, there will be a force in vertical direction:  $F_4$

We can get the value of angle  $\varphi$ :  $\varphi = 15^\circ$

$$F_4 = F_{3*} \times \sin 15 = 0.188N$$

$$F_5 = F_{3*} \times \cos 15 = 0.7N$$

$$F_n = 2.054N$$

$$F_b = 1.96N$$

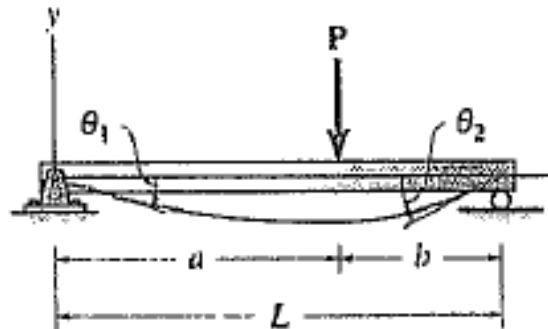
$$M_{max} = 0.2698Nm$$

$$\sigma = M \times y \div I_z$$

$$I_z = 1.055 \times 10^{-11}m^4$$

$$\sigma_{max} = 16.5MPa$$

$$\tau_{max} = \frac{V_{max}}{A} = \frac{2.054}{3.738 \times 10^{-6}} = 0.55MPa$$



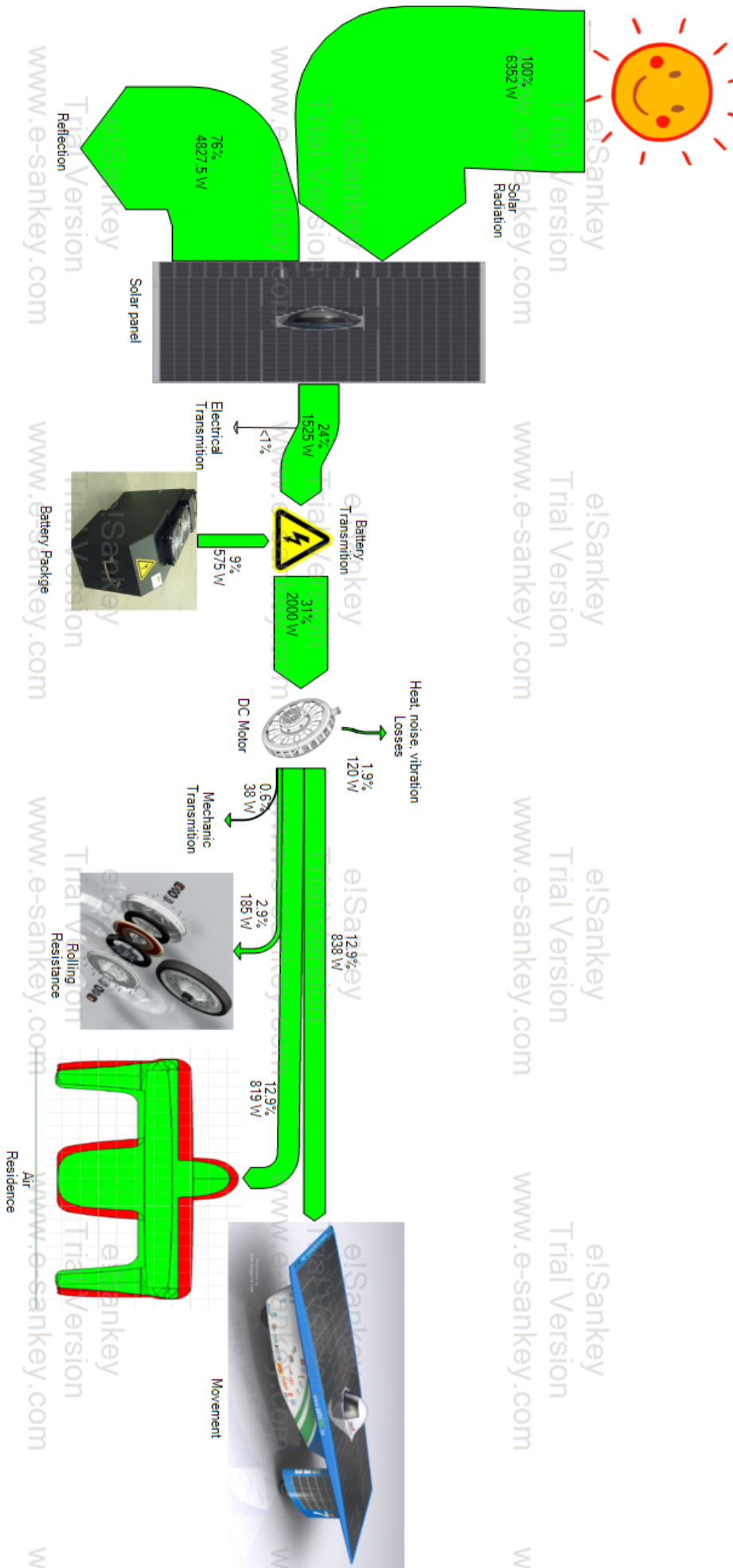
In the direction of  $F_4$ , because of its value is much smaller than the value of vertical direction. So we don't need to calculate it!

We have check the normal stress and shear stress of Aluminum. Our value form our calculation is smaller than data value. So our design is safe.

Data from

<http://www.matweb.com/search/DataSheet.aspx?MatGUID=e5de9f1161d34f71a34ae016723d097f&ckck=1>

## 2.Sankey diagram



This Sankey diagram shows us all the power losses in the Umicar, when racing in the top speed with batteries.

Here is the all value that be used during the calculation.

Mass:	225kg
Rolling resistance coefficient:	$C_{rr} = 0.0025$ (theoretical, on 8 bar tire pressure)
$C_{rr} = 0.0056$ (experimental, on 5 bar tire pressure)	
Average motor efficiency:	94%
Average controller efficiency:	99%
280 RWE solar cells:	30% average efficiency
2576 Emcore solar cells:	24.5% average efficiency
Frontal Area:	$0.81\text{m}^2$
Max Speed on Batteries:	$75\text{mph} = 33.54\text{m/s}$
Active Area:	$7.94\text{m}^2$
Panel Conversion Efficiency:	24%
Array Voltage:	100V
Density of air:	$\rho = 1,293 \text{ kg/m}^3$
<b>MOTOR AT DESIGN OPERATING POINT:</b>	
Efficiency:	94%
Battery Pack Voltage:	96V

## Calculations:

Solar radiation(100%):

$$\frac{800\text{w}}{\text{m}^2} * 7.94\text{m}^2 = 6352\text{w}$$

Reflection(76%):

$$6352\text{w} * 76\% = 4827.5\text{w}$$

Solar → Storage battery(24%):

$$6352\text{w} * 24\% = 1525\text{w}$$

Storage battery → DC motor(29.1%):

$$94\% * 31\% = 29.1\%$$

$$29.1\% * 6352\text{w} = 1848\text{w}$$

Mechanical Transmission losses(0.6%):

$$29.1\% * 2\% = 0.6\%$$

$$0.6\% * 6352\text{w} = 3811\text{w}$$

Rolling resistance(2.9%):

$$P_r = F_r * V_{\text{max}} = m * g * v * C_r = 185\text{w}$$

$$\frac{185\text{w}}{6352\text{w}} = 2.9\%$$

Air resistance(12.9%):

$$P_{\text{air}} = F_{\text{air}} * V_{\text{max}} = \frac{1}{2} * C_w * A * \rho * v^3 = 819\text{w}$$

$$\frac{819\text{w}}{6352\text{w}} = 12.9\%$$